

Occasionally Weakly Compatible Mappings

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Abstract In this paper, the concept of compatible maps of type (A) and occasionally weakly compatible maps in fuzzy metric space have been applied to prove common fixed point theorem. A fixed point theorem for six self maps has been established using the concept of compatible maps of type (A) and occasionally weakly compatible maps, which generalizes the result of Cho [16].

Keywords: common fixed points, fuzzy metric space, compatible maps, compatible maps of type (A) and occasionally weakly compatible maps

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1. Introduction

The concept of Fuzzy sets was initially investigated by Zadeh [13] as a new way to represent vagueness in everyday life. Subsequently, it was developed by many authors and used in various fields. To use this concept in Topology and Analysis, several researchers have defined Fuzzy metric space in various ways. In this paper we deal with the Fuzzy metric space defined by Kramosil and Michalek [11] and modified by George and Veeramani [20]. Recently, Grebiec [1] has proved fixed point results for Fuzzy metric space. In the sequel, Singh and Chauhan [12] introduced the concept of compatible mappings of Fuzzy metric space and proved the common fixed point theorem. Jungck et. al. [2] introduced the concept of compatible maps of type (A) in metric space and proved fixed point theorems. Using the concept of compatible maps of type (A), Jain et. al. [18] proved a fixed point theorem for six self maps in a fuzzy metric space. Singh et. al. [7,8] proved fixed point theorems in a fuzzy metric space. Recently in 2012, Jain et. al. [4,5] and Sharma et. al. [6] proved various fixed point theorems using the concepts of semi-compatible mappings, property (E.A.) and absorbing mappings. The concept of occasionally weakly compatible mappings in metric spaces is introduced by Al-Thagafi and Shahzad [14] which is most general among all the commutativity concepts. Recently, Khan and Sumitra [15] extended the notion of occasionally weakly compatible maps to fuzzy metric space.

In this paper, a fixed point theorem for six self maps has been established using the concept of compatible maps of type (A) occasionally weakly compatible mappings, which generalizes the result of Cho [16].

For the sake of completeness, we recall some definitions and known results in Fuzzy metric space.

2. Definitions, lemmas, Remarks, Propositions

Definition 2.1. [10] A binary operation $*$: $[0,1] \times [0,1] \rightarrow [0,1]$ is called a t -norm if $([0,1], *)$ is an abelian topological monoid with unit 1 such that $a * b \leq c * d$. Whenever $a \leq c$ and $b \leq d$ for $a, b, c, d \in [0,1]$.

Examples of t -norms are:

$$a * b = ab \text{ and } a * b = \min \{a, b\}.$$

Definition 2.2. [10] The 3-tuple $(X, M, *)$ is said to be a Fuzzy metric space if X is an arbitrary set, $*$ is a continuous t -norm and M is a Fuzzy set in $x^2 \times [0, \infty)$ satisfying the following conditions:

For all $x, y, z \in X$ and $s, t > 0$

(FM-1) $M(x, y, 0) = 0$,

(FM-2) $M(x, y, t) = 1$ for all $t > 0$ iff $x = y$,

(FM-3) $M(x, y, t) = M(y, x, t)$,

(FM-4) $M(x, y, t) * M(y, z, s) = M(x, z, t + s)$,

(FM-5) $M(x, y, \cdot) : [0, \infty) \rightarrow [0, 1]$ is left continuous,

(FM-6) $\lim_{n \rightarrow \infty} M(x, y, t) = 1$

Note that $M(x, y, t)$ can be considered as the degree of nearness between x and y with respect to t . We identify $x = y$ with $M(x, y, t) = 1$ for all $t > 0$. The following example shows that every metric space induces a Fuzzy metric space.

Example 2.1. [10] Let (X, d) be a metric space. Define $a * b = \min \{a, b\}$ and $M(x, y, t) = \frac{t}{t + d(x, y)}$ for all

$x, y \in X$ and $t > 0$. Then $(X, M, *)$ is a Fuzzy metric space. It is called the Fuzzy metric space induced by d .

Definition 2.3. [10] A sequence $\{x_n\}$ in a Fuzzy metric space $(X, M, *)$ is said to be a Cauchy sequence if and only if for each $\varepsilon > 0, t > 0$, there exists $n_0 \in \mathbb{N}$ such that $M(X_n, X_m, t) > 1 - \varepsilon$ for all $n, m \geq n_0$.

The sequence $\{x_n\}$ is said to converge to a point x in X if and only if for each $\varepsilon > 0, t > 0$ there exists $n_0 \in \mathbb{N}$ such that $M(x_n, x, t) > 1 - \varepsilon$ for all $n, m \geq n_0$.

A Fuzzy metric space $(X, M, *)$ is said to be complete if every Cauchy sequence in it converges to a point in it.

Definition 2.4. [12] Self mappings A and S of a Fuzzy metric space $(X, M, *)$ are said to be compatible if and only if $M(ASx_n, SAx_n, t) \rightarrow 1$ for all $t > 0$, whenever $\{x_n\}$ is a sequence in X such that $Sx_n, Ax_n \rightarrow p$ for some p in X as $n \rightarrow \infty$.

Definition 2.5. [18] Self maps A and S of a Fuzzy metric space $(X, M, *)$ are said to be compatible maps of type (A) if $M(ASx_n, SSx_n, t) \rightarrow 1$ and $M(SAx_n, AAx_n, t) \rightarrow 1$ for all $t > 0$, whenever $\{x_n\}$ is a sequence in X such that $Sx_n, Ax_n \rightarrow p$ for some p in X as $n \rightarrow \infty$.

Definition 2.6. [15] Two maps A and S from a Fuzzy metric space $(X, M, *)$ into itself are said to be Occasionally weakly compatible (owc) if and only if there is a point $x \in X$, which is coincidence point of A and S at which A and S commute.

Remark 2.1. [18] The concept of compatible maps of type (A) and occasionally weakly compatibility is more general than the concept of compatible maps in a Fuzzy metric space.

Proposition 2.1. [18] In a Fuzzy metric space $(X, M, *)$ limit of a sequence is unique.

Lemma 2.1. [1] Let $(X, M, *)$ be a fuzzy metric space. Then for all $x, y \in X, M(x, y, \cdot)$ is a non-decreasing function.

Lemma 2.2. [16] Let $(X, M, *)$ be a fuzzy metric space. If there exists $k \in (0, 1)$ such that for all $x, y \in X, M(x, y, kt) \geq M(x, y, t) \forall t > 0$, then $x = y$.

Lemma 2.3. [18] Let $\{x_n\}$ be a sequence in a fuzzy metric space $(X, M, *)$. If there exists a number $k \in (0, 1)$ such that $M(x_{n+2}, x_{n+1}, kt) \geq M(x_{n+1}, x_n, t) \forall t > 0$ and $n \in \mathbb{N}$. Then $\{x_n\}$ is a Cauchy sequence in X .

Proposition 2.2. [18] Let A and S be concept of compatible maps of type (A) of a complete fuzzy metric space $(X, M, *)$ with continuous t -norm $*$ defined by $a * b = \min\{a, b\}$ for all $a, b \in [0, 1]$ and $Su = Tu$ for some u in X . Then $STu = TSu = SSu = TTu$.

Lemma 2.4. [3] The only t -norm $*$ satisfying $r * r \geq r$ for all $r \in [0, 1]$ is the minimum t -norm, that is $a * b = \min\{a, b\}$ for all $a, b \in [0, 1]$.

3. Main Result

Theorem 3.1. Let $(X, M, *)$ be a complete fuzzy metric space and let A, B, S, T, P and Q be mappings from X into itself such that the following conditions are satisfied:

- (a) $P(X) \subset ST(X), Q(X) \subset AB(X)$;
- (b) $AB = BA, ST = TS, PB = BP, QT = TQ$;
- (c) either P or AB is continuous;

(d) (P, AB) is compatible maps of type (A) and (Q, ST) is occasionally weakly compatible ;

(e) there exists $q \in (0, 1)$ such that for every $x, y \in X$ and $t > 0$

$$M(Px, Qy, qt) \geq M(ABx, STy, *M(Px, ABx, t)v * M(Qy, STy, t * M(Px, STy, t)).$$

Then A, B, S, T, P and Q have a unique common fixed point in X .

Proof: Let $x_0 \in X$. From (a) there exist $x_1, x_2 \in X$ such that $Px_0 = STx_1$ and $x_1 = ABx_2$.

Inductively, we can construct sequences $\{x_n\}$ and $\{y_n\}$ in X such that $Px_{2n-2} = STx_{2n-1} = y_{2n-1}$ and $Qx_{2n-1} = ABx_{2n} = y_{2n}$ for $n = 1, 2, 3, \dots$

Step 1. Put $x = x_{2n}$ and $y = x_{2n+1}$ in (e), we get

$$\begin{aligned} &M(Px_{2n}, Qx_{2n+1}, qt) \\ &\geq M(ABx_{2n}, STx_{2n+1}, t) * M(Px_{2n}, ABx_{2n}, t) \\ &\quad * M(Qx_{2n+1}, STx_{2n+1}, t) * M(Px_{2n}, STx_{2n+1}, t). \\ &= M(y_{2n}, y_{2n+1}, t) * M(y_{2n+1}, y_{2n}, t) \\ &\quad * M(y_{2n+2}, y_{2n+1}, t) * M(y_{2n+1}, y_{2n+1}, t) \\ &\geq M(y_{2n}, y_{2n+1}, t) * M(y_{2n+1}, y_{2n+2}, t). \end{aligned}$$

From lemma 2.1 and 2.2, we have

$$M(y_{2n+1}, y_{2n+2}, qt) \geq M(y_{2n}, y_{2n+1}, t).$$

Similarly, we have

$$M(y_{2n+2}, y_{2n+3}, qt) \geq M(y_{2n+1}, y_{2n+2}, t).$$

Thus, we have

$$M(y_{n+1}, y_{n+2}, qt) \geq M(y_n, y_{n+1}, t) \text{ for } n = 1, 2, \dots$$

$$\begin{aligned} M(y_n, y_{n+1}, t) &\geq M(y_n, y_{n+1}, t/q) \\ &\geq M(y_{n-2}, y_{n-1}, t/q^2) \\ &\dots \dots \dots \\ &\geq M(y_1, y_2, t/q^n) \rightarrow 1 \text{ as } n \rightarrow \infty, \end{aligned}$$

and hence $M(y_n, y_{n+1}, t) \rightarrow 1$ as $n \rightarrow \infty$ for any $t > 0$.

For each $\varepsilon > 0$ and $t > 0$, we can choose $n_0 \in \mathbb{N}$ such that

$$M(y_n, y_{n+1}, t) > 1 - \varepsilon \text{ for all } n > n_0.$$

For $m, n \in \mathbb{N}$, we suppose $m \geq n$. Then we have

$$\begin{aligned} &M(y_n, y_m, t) \geq M(y_n, y_{n+1}, t/m-n) \\ &\quad * M(y_{n+1}, y_{n+2}, t/m-n) \\ &\quad * \dots * M(y_{m-1}, y_m, t/m-n) \\ &\geq (1-\varepsilon) * (1-\varepsilon) * \dots * (1-\varepsilon) \\ &\hspace{15em} (m-n) \text{ times} \end{aligned}$$

$$M(y_n, y_m, t) \geq (1-\varepsilon)$$

and hence $\{y_n\}$ is a Cauchy sequence in X .

Since $(X, M, *)$ is complete, $\{y_n\}$ converges to some point $z \in X$. Also its subsequence's converges to the same point i.e. $z \in X$

$$\text{i.e., } \{Qx_{2n+1}\} \rightarrow z \text{ and } \{STx_{2n+1}\} \rightarrow z \tag{1}$$

$$\{Px_{2n}\} \rightarrow z \text{ and } \{ABx_{2n}\} \rightarrow z. \tag{2}$$

Case I. Suppose AB is continuous.

Since AB is continuous, we have

$$(AB)^2x_{2n} \rightarrow ABz \text{ and } ABPx_{2n} \rightarrow ABz.$$

As (P, AB) is compatible pair of type (A) , we have $PABx_{2n} \rightarrow ABz$.

Step 2. Put $x = ABx_{2n}$ and $y = x_{2n+1}$ in (e), we get

$$\begin{aligned} & M(PABx_{2n}, Qx_{2n+1}, qt) \\ & \geq M(ABABx_{2n}, STx_{2n+1}, t) * M(PABx_{2n}, ABABx_{2n}, t) \\ & \quad * M(Qx_{2n+1}, STx_{2n+1}, t) * M(PABx_{2n}, STx_{2n+1}, t). \end{aligned}$$

Taking $\rightarrow \infty$, we get

$$\begin{aligned} M(ABz, z, qt) & \geq M(ABz, z, t) * M(ABz, ABz, \\ & \quad * M(z, z, t) * M(ABz, z, t) \\ & \geq M(ABz, z, t) * M(ABz, z, t) \end{aligned}$$

$$i. e. M(ABz, z, qt) \geq M(ABz, z, t).$$

Therefore, by using lemma 2.2, we get

$$ABz = z. \quad (3)$$

Step 3. Put $x = z$ and $y = x_{2n+1}$ in (e), we have

$$\begin{aligned} & M(Pz, Qx_{2n+1}, qt) \\ & \geq M(ABz, STx_{2n+1}, t) * M(Pz, ABz, t) \\ & \quad * M(Qx_{2n+1}, STx_{2n+1}, t) * M(Pz, STx_{2n+1}, t). \end{aligned}$$

Taking $n \rightarrow \infty$ and using equation (1), we get

$$\begin{aligned} M(Pz, z, qt) & \geq M(z, z, t) * M(Pz, z, t) \\ & \quad * M(z, z, t) * M(Pz, z, t) \\ & \geq M(Pz, z, t) * M(Pz, z, t) \end{aligned}$$

$$i. e. M(Pz, z, qt) \geq M(Pz, z, t).$$

Therefore, by using lemma 2.2, we get

$$Pz = z. \text{ Therefore, } ABz = Pz = z.$$

Step 4. Putting $x = Bz$ and $y = x_{2n+1}$ in condition (e), we get

$$\begin{aligned} & M(PBz, Qx_{2n+1}, qt) \\ & \geq M(ABBz, STx_{2n+1}, t) * M(PBz, ABBz, t) \\ & \quad * M(Qx_{2n+1}, STx_{2n+1}, t) * M(PBz, STx_{2n+1}, t). \end{aligned}$$

As $BP = PB, AB = BA$, so we have

$$\begin{aligned} P(Bz) & = B(Pz) = Bz \text{ and } (AB)(Bz) \\ & = (BA)(Bz) = B(ABz) = Bz. \end{aligned}$$

Taking $n \rightarrow \infty$ and using (1), we get

$$\begin{aligned} & M(Bz, z, qt) \\ & \geq M(Bz, z, t) * M(Bz, Bz, t) * M(z, z, t) * M(Bz, z, t) \\ & \geq M(Bz, z, t) * M(Bz, z, t) \end{aligned}$$

$$i. e. M(Bz, z, qt) \geq M(Bz, z, t).$$

Therefore, by using lemma 2.2, we get

$$Bz = z \text{ and also we have } ABz = z \Rightarrow Az = z.$$

Therefore,

$$Az = Bz = Pz = z \quad (4)$$

Step 5. As $P(X) \subset ST(X)$, there exists $u \in X$ such that $z = Pz = STu$.

Putting $x = x_{2n}$ and $y = u$ in (e), we get

$$\begin{aligned} & M(Px_{2n}, Qu, qt) \\ & \geq M(ABx_{2n}, STu, t) * M(Px_{2n}, ABx_{2n}, t) \\ & \quad * M(Qu, STu, t) * M(Px_{2n}, STu, t). \end{aligned}$$

Taking $n \rightarrow \infty$ and using (1) and (2), we get

$$\begin{aligned} M(z, Qu, qt) & \geq M(z, z, t) * M(z, z, t) \\ & \quad * M(Qu, z, t) * M(z, z, t) * M(z, z, t) \\ & \geq M(Qu, z, t) \end{aligned}$$

$$i. e. M(z, Qu, qt) \geq M(z, Qu, t).$$

Therefore, by using lemma 2.2, we get $Qu = z$. Hence $STu = z = Qu$. Since (Q, ST) is occasionally weakly compatible, therefore, by proposition (2.2), we have

$$QSTu = STQu. \text{ Thus } Qz = STz.$$

Step 6. Putting $x = x_{2n}$ and $y = z$ in (e), we get

$$\begin{aligned} & M(Px_{2n}, Qz, qt) \\ & \geq M(ABx_{2n}, STz, t) * M(Px_{2n}, ABx_{2n}, t) \\ & \quad * M(Qz, STz, t) * M(Px_{2n}, STz, t). \end{aligned}$$

Taking $n \rightarrow \infty$ and using (2) and step 5, we get

$$\begin{aligned} M(z, Qz, qt) & \geq M(z, Qz, t) * M(z, z, t) \\ & \quad * M(Qz, Qz, t) * M(z, Qz, t) \\ & \geq M(z, Qz, t) * M(z, Qz, t) \end{aligned}$$

$$i. e. M(z, Qz, qt) \geq M(z, Qz, t).$$

Therefore, by using lemma 2.2, we get

$$Qz = z.$$

Step 7. Putting $x = x_{2n}$ and $y = Tz$ in (e), we get

$$\begin{aligned} & M(Px_{2n}, QTz, qt) \\ & \geq M(ABx_{2n}, STTz, t) * M(Px_{2n}, ABx_{2n}, t) \\ & \quad * M(QTz, STTz, t) * M(Px_{2n}, STTz, t). \end{aligned}$$

As $QT = TQ$ and $ST = TS$, we have

$$\begin{aligned} QTz & = TQz = Tz \\ \text{and } ST(Tz) & = T(STz) = TQz = Tz. \end{aligned}$$

Taking $n \rightarrow \infty$, we get

$$\begin{aligned} M(z, Tz, qt) & \geq M(z, Tz, t) * M(z, z, t) \\ & \quad * M(Tz, Tz, t) * M(z, Tz, t) \\ & \geq M(z, Tz, t) * M(z, Tz, t) \end{aligned}$$

$$i. e. M(z, Tz, qt) \geq M(z, Tz, t)$$

Therefore, by using lemma 2.2, we get

$$Tz = z. \text{ Now } STz = Tz = z \text{ implies } Sz = z.$$

Hence

$$Sz = Tz = Qz = z. \quad (5)$$

Combining (4) and (5), we get

$$Az = Bz = Pz = Qz = Tz = Sz = z.$$

Hence, z is the common fixed point of A, B, S, T, P and Q .

Case II. Suppose P is continuous.

As P is continuous,

$$P^2x_{2n} \rightarrow Pz \text{ and } P(AB)x_{2n} \rightarrow Pz.$$

As (P, AB) is compatible pair of type (A) , $(AB)Px_{2n} \rightarrow Pz$.

Step 8. Putting $x = Px_{2n}$ and $y = x_{2n+1}$ in condition (e), we have

$$\begin{aligned} &M(PPx_{2n}, Qx_{2n+1}, qt) \\ &\geq M(ABPx_{2n}, STx_{2n+1}, t) * M(PPx_{2n}, ABPx_{2n}, t) \\ &\quad * M(Qx_{2n+1}, STx_{2n+1}, t) * M(PPx_{2n}, STx_{2n+1}, t). \end{aligned}$$

Taking $n \rightarrow \infty$, we get

$$\begin{aligned} M(Pz, z, qt) &\geq M(Pz, z, t) * M(Pz, Pz, t) \\ &\quad * M(z, z, t) * M(Pz, z, t) \\ &\geq M(Pz, z, t) * M(Pz, z, t) \end{aligned}$$

i.e. $M(Pz, z, qt) \geq M(Pz, z, t)$.

Therefore by using lemma 2.2, we have

$$Pz = z.$$

Further, using steps 5,6,7, we get

$$Qz = STz = Sz = Tz = z.$$

Step 9. As $Q(X) \subset AB(X)$, there exists $w \in X$ such that $z = Qz = ABw$

Put $x = w$ and $y = x_{2n+1}$ in (e), we get

$$\begin{aligned} &M(Pw, Qx_{2n+1}, qt) \\ &\geq M(ABw, STx_{2n+1}, t) * M(Pw, ABw, t) \\ &\quad * M(Qx_{2n+1}, STx_{2n+1}, t) * M(Pw, STx_{2n+1}, t). \end{aligned}$$

Taking $n \rightarrow \infty$, we get

$$\begin{aligned} M(Pw, z, qt) &\geq M(z, z, t) * M(Pw, z, t) \\ &\quad * M(z, z, t) * M(Pw, z, t) \\ &\geq M(Pw, z, t) * M(Pw, z, t) \end{aligned}$$

i.e. $M(Pw, z, qt) \geq M(Pw, z, t)$.

Therefore, by using lemma 2.2, we get

$$Pw = z. \text{ Therefore, } ABw = z = Pw.$$

As (P, AB) is compatible pair of type (A) , then by proposition (2.2), we have

$$Pz = ABz.$$

Also, from step 4, we get $Bz = z$.

$$Az = Bz = Pz = z.$$

Further, using steps 5, 6, 7, we get

$$Qz = STz = Sz = Tz = z$$

i.e. z is the common fixed point of the six maps A, B, S, T, P and Q in this case also.

Uniqueness: Let u be another common fixed point of A, B, S, T, P and Q .

Then $Au = Bu = Pu = Qu = Su = Tu = u$.

Put $x = z$ and $y = u$ in (e), we get

$$\begin{aligned} M(Pz, Qu, qt) &\geq M(ABz, STu, t) * M(Pz, ABz, t) \\ &\quad * M(Qu, STu, t) * M(Pz, STu, t). \end{aligned}$$

Taking $n \rightarrow \infty$, we get

$$\begin{aligned} M(z, u, qt) &\geq M(z, u, t) * M(z, z, t) \\ &\quad * M(u, u, t) * M(z, u, t) \\ &\geq M(z, u, t) * M(z, u, t) \end{aligned}$$

i.e. $M(z, u, qt) \geq M(z, u, t)$.

Therefore by using lemma (2.2), we get $z = u$.

Therefore z is the unique common fixed point of self maps A, B, S, T, P and Q .

Remark 3.1. If we take $B = T = I$, the identity map on X in theorem 3.1, then condition (b) is satisfied trivially and we get

Corollary 3.1. Let $(X, M, *)$ be a complete fuzzy metric space and let A, S, P and Q be mappings from X into itself such that the following conditions are satisfied:

- (a) $P(X) \subset S(X), Q(X) \subset A(X)$;
- (b) either A or P is continuous;
- (c) (P, A) is compatible maps of type (A) and (Q, S) is occasionally weakly compatible;
- (d) there exists $q \in (0, 1)$ such that for every $x, y \in X$ and $t > 0$

$$\begin{aligned} M(Px, Qy, qt) &\geq M(Ax, Sy, t) * M(Px, Ax, t) \\ &\quad * M(Qy, Sy, t) * M(Px, Sy, t). \end{aligned}$$

Then A, S, P and Q have a unique common fixed point in X .

Remark 3.2. In view of remark 3.1, corollary 3.1 is a generalization of the result of Cho [16] in the sense that condition of compatibility of the pairs of self maps has been restricted to compatibility of type (A) occasionally weakly compatible and only one map of the first pair is needed to be continuous.

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