Estimation of E-Field inside Muscle Tissue at MICS and ISM Frequencies Using Analytic and Numerical Methods

Yessar E. Mohammed¹, Ali G. Saber²*

¹Department of Electrical Engineering, University of Mosul, College of Engineering, Mosul, Iraq
²Department Electrical Engineering, University of Mosul, College of Engineering, Mosul, Iraq

*Corresponding author: alicce2006@gmail.com

Received May 16, 2014; Revised June 04, 2014; Accepted November 07, 2014

Abstract This paper presents studying for analytic and numerical methods which are used for evaluating the magnitude of electric field inside human tissues for different depths and using the most important frequencies in medical application fields, then showing the difference range between the two methods. The first method considers the human tissue as one-dimensional layered, the layers in this method modeled with non uniform transmission line. The second method is using numerical simulation CST Microwave Studio which considers the human tissues as 3D-dimensional layered. This paper also investigates the penetration for the magnitude of electric field into the phantom model of human tissues, especially into muscle tissue using different frequencies and how the electric field behaves inside the tissue when the penetration depth greater than the thickness of the tissue, as well as when the penetration depth smaller than the thickness of the tissue.

Keywords: electric field, penetrating depth, muscle tissue, medical applications, ISM, MICS


1. Introduction

Over the last decades several techniques have been developed to analyze interactions between incident electromagnetic wave and human tissue, generally the human tissue divided into multilayer [1,2]. The electric properties of human tissue vary with frequency changing [3,4,5]. There are many bands used in the medical fields. In this research study focused on MICS Medical Implant Communication System (402MHz) and ISM (Industrial Scientific and Medical) bands which commonly used in the diagnostic and therapeutic applications. ISM bands were originally reserved internationally for the use of RF electromagnetic fields for industrial, scientific and medical purposes other than communications, ISM includes the frequencies (434MHz, 915MHz, 2.45MHz, 5.8GHz) [9,10,11,12,13]. The main purpose of the recent researches is estimating the specific absorption rate (SAR) in the tissues [14,15]. For evaluating SAR at certain depth, we need to find E-field at certain frequency and apply equation (1) [16].

\[ \text{SAR} = \frac{\sigma E^2}{\rho} \left( \frac{W}{kg} \right) \]

where \( \sigma \) represents the conductivity of tissue (S/m), \( \rho \) the density of the tissue (kg/m³) and \( E \) the electric field (V/m). There are many applications for evaluating the E-field. The most three important applications are [6].

- Therapeutic applications, such as hyperthermia by focusing EM-field at certain point.
- Diagnostic applications, EM-fields at microwave frequencies can provide a convenient approach to detect and monitor physiological.
- Studying the effects of Electromagnetic that penetrates the tissue such as using mobile and microwave frequency.

There are several methods for evaluating the electric field in biological tissue. The simple method considers the tissue as homogeneous medium, then by analyzing the transmission characteristics of multilayer structure using non uniform transmission line method [6,7,8], where the characteristic impedances and transmission coefficients of each layers are calculated, then applying the non uniform transmission line method to calculate the parameter of ABCD network [6,7,8]. Other method is using CST software for evaluating the electric field inside human tissue. The CST software applies FIT technique (Finite Integration Technique). This paper gives interesting for evaluating the magnitude of E-field inside muscle tissue, at different points, and at different frequencies with using two methods. The main reason of choosing muscle tissue is the wide thickness of this tissue [1,2]. Thus, the study will be more clarity. The methods which presented in this paper can be used to evaluate the magnitude of E-field inside another tissue.

2. Characteristics of Human Tissues
According to previous research, the electrical properties of human tissue are changing with frequency. There is a database available for most parameters of tissues [3,4]. Table 1, includes information for several tissues and at four frequencies [3]. The penetration depth can be obtained from database [3,4] or by applying equation(2) [17].

\[
\delta = \frac{1}{\omega} \left[ \left( \frac{\mu_0 \epsilon_0 \sigma_e}{2} \right)^2 + \left( \frac{\sigma}{\omega \mu_0 \epsilon_0} \right)^2 \right]^{-1/2}
\]

(2)

Where: \( \mu_0 \) free space electromagnetic permeability, \( \epsilon_0 \) free space permittivity, \( \sigma_e \) relative permittivity of the tissue, \( \omega \) wave pulsation, and \( \delta \) the penetration depth.

Table 1. Electric Properties of Human Tissue at Different Frequencies [3]

<table>
<thead>
<tr>
<th>Frequency</th>
<th>Tissue parameters</th>
<th>Dry skin</th>
<th>Fat</th>
<th>Muscle</th>
<th>Bone</th>
</tr>
</thead>
<tbody>
<tr>
<td>402MHz</td>
<td>( \sigma ) (S/m)</td>
<td>0.688</td>
<td>0.041</td>
<td>0.796</td>
<td>0.091</td>
</tr>
<tr>
<td></td>
<td>( \epsilon_r )</td>
<td>46.74</td>
<td>5.578</td>
<td>57.11</td>
<td>13.14</td>
</tr>
<tr>
<td></td>
<td>Penetration depth (mm)</td>
<td>55.22</td>
<td>308.7</td>
<td>52.55</td>
<td>212.8</td>
</tr>
<tr>
<td>915MHz</td>
<td>( \sigma ) (S/m)</td>
<td>0.871</td>
<td>0.051</td>
<td>0.948</td>
<td>0.1451</td>
</tr>
<tr>
<td></td>
<td>( \epsilon_r )</td>
<td>41.33</td>
<td>5.457</td>
<td>54.99</td>
<td>12.44</td>
</tr>
<tr>
<td></td>
<td>Penetration depth (mm)</td>
<td>39.95</td>
<td>242.3</td>
<td>42.1</td>
<td>129.8</td>
</tr>
<tr>
<td>2.45GHz</td>
<td>( \sigma ) (S/m)</td>
<td>1.464</td>
<td>0.1045</td>
<td>1.7388</td>
<td>0.3943</td>
</tr>
<tr>
<td></td>
<td>( \epsilon_r )</td>
<td>22.57</td>
<td>5.280</td>
<td>52.73</td>
<td>11.38</td>
</tr>
<tr>
<td></td>
<td>Penetration depth (mm)</td>
<td>3.717</td>
<td>4.954</td>
<td>4.9615</td>
<td>1.1544</td>
</tr>
<tr>
<td>5.8GHz</td>
<td>( \sigma ) (S/m)</td>
<td>35.11</td>
<td>4.594</td>
<td>4.9615</td>
<td>1.1544</td>
</tr>
<tr>
<td></td>
<td>( \epsilon_r )</td>
<td>8.573</td>
<td>40.48</td>
<td>7.541</td>
<td>14.539</td>
</tr>
</tbody>
</table>

Table 1 shows the penetration depth of tissues versus frequency. To penetrate any tissue the penetration depth must be greater than thickness of that tissue.

The electric field strength decreases according to the equation (3) [18].

\[
E = E_0 e^{-\frac{z}{\delta}}
\]

(3)

Where: \( E \) electric field at certain point, \( E_0 \) reference electric field, \( z \) distance from \( E_0 \). Inside tissue the E-field will be combining of the wave arrived and the reflected wave from next tissue as in equation (4) [18].

\[
E = E_0 (e^{-\frac{z}{\delta}} + \Gamma e^{\frac{z}{\delta}})
\]

(4)

Where \( \Gamma \) represents the reflection coefficient of next tissue, there are more than one reflection accrues inside each tissue, therefore, the matter will be more complicated.

3. Analytic Calculation and Numerical Simulation

3.1. First Method

This method considers the human tissues as non uniform transmission lines. The characteristic impedance and transmission coefficient of each tissue can be calculated from equation(5)(6) respectively [6,7,8].

\[
Z_i = \sqrt{\frac{j \omega \mu_i}{\sigma + j \omega \epsilon_i}}
\]

(5)

\[
\gamma_i = \sqrt{j \omega \mu_i (\sigma_i + j \omega \epsilon_i)}
\]

(6)

Where \( Z_i \) and \( \gamma_i \) are characteristic impedance and transmission coefficient of each layer respectively.

For applying this method we will consider the layers of human as one-dimensional layers as shown in Fig. 2: where Db thickness of bone (20mm), Dm thickness of muscle (20mm), Df thickness of fat (4mm), Ds thickness of skin (2mm), and Dfs free space distance between source and surface of skin layer (10mm), then calculating the parameter of ABCD network using the network parameter matrix of non uniform transmission line in equation (7) [6,7,8].

\[
\begin{bmatrix}
A_1 & A_2 \\
A_3 & A_4
\end{bmatrix}
= \prod_{i=1}^{m} \begin{bmatrix}
\cosh \gamma_i l_i & Z_i \sinh \gamma_i l_i \\
\sinh \gamma_i l_i & \cosh \gamma_i l_i
\end{bmatrix}
\]

(7)
Where \( m \) represents number of tissues, \( l_i \) the thickness of each tissue. The magnitude of E-field and the impedance of tissue (\( Z_i \)) at distance \( l \) to the next tissue can be calculated using equations (8)(9) respectively [6,7,8]. Where \( Z_b \) free space impedance, \( Z_m \) impedance of bone, \( E_0 \) incident signal perpendicular to skin, and calculating by equation (9) [6,7,8].

\[
|E|_{l_{i-1}} = \left| \frac{2Z_l}{A_2Z_lZ_{l_d} + A_4Z_{l_d} + A_1Z_l + A_2} \right| E_0
\]  

(8)

\[
Z_{m} = \frac{Z_b + Z_m \tanh \gamma_m l}{Z_m + Z_b \tanh \gamma_m l}
\]  

(9)

Where: \( Z_m \) impedance of muscle tissue, \( \gamma_m \) transmission coefficient of muscle tissue, and \( Z_{m}^{l_{i}} \) input impedance of part of muscle at distance \( l \) to bone tissue.

### 3.2. Second Method

This method uses CST Microwave Studio which applies Finite Integration Technique. The body phantom designed with dimensions 40mm × 40mm. The structure of phantom model consists of four layers with the same thickness that used in first method. Figure 3 includes the structures of the body phantom that used in this paper.

### 4. Results and Comparison

To compare the results which obtained from the two methods, the tissue parameters, and dimensions should be the same in two methods. The depth into muscle tissue where chosen for comparison at 4, 8, 10, 12, 14 and 18mm. The magnitude of E-field of these points has been calculated for different frequency with normal incident E-field 10V/m to phantom model. For plotting the results we should take more points, therefore, the magnitude of E-field will calculate at each 0.25mm into muscle tissue. When using plane wave with frequency 402MHz, 915MHz and 2.45GHz, the penetration depth of each tissue which used greater than it’s thickness, therefore, the signal will penetrate the tissue and reflect from next tissue, causing fluctuation at different point, then forming standing wave. The results are illustrating in Figure 4-a, Figure 4-b, Figure 5-a, Figure 5-b, Figure 6-a and Figure 6-b. The comparison of two methods at different depths and different frequencies illustrated in Table 2, Table 3, Table 4, and Table 5.

<table>
<thead>
<tr>
<th>Table 2. Comparison between two method at 402MHz</th>
</tr>
</thead>
<tbody>
<tr>
<td>Depth (mm)</td>
</tr>
<tr>
<td>Method 1 (V/m)</td>
</tr>
<tr>
<td>Method 2 (V/m)</td>
</tr>
</tbody>
</table>

<table>
<thead>
<tr>
<th>Table 3. Comparison between two method at 915MHz</th>
</tr>
</thead>
<tbody>
<tr>
<td>Depth (mm)</td>
</tr>
<tr>
<td>Method 1 (V/m)</td>
</tr>
<tr>
<td>Method 2 (V/m)</td>
</tr>
</tbody>
</table>

<table>
<thead>
<tr>
<th>Table 4. Comparison between two method at 2.45GHz</th>
</tr>
</thead>
<tbody>
<tr>
<td>Depth (mm)</td>
</tr>
<tr>
<td>Method 1 (V/m)</td>
</tr>
<tr>
<td>Method 2 (V/m)</td>
</tr>
</tbody>
</table>

Figure 4-a. Distribution of magnitude of E-field inside muscle tissue using first method at 402MHz; 4-b. Distribution of magnitude of E-field inside muscle tissue using second method at 402MHz.
When using plane wave of 5.8GHz, the penetration depth according to equation (2) is 7.5413mm. The thickness of muscle tissue that used in this paper 20mm, δ < thickness, therefore, the reflected signal from next tissue will be very small causing exponential fading of signal especially for region from the beginning of the muscle tissue to a depth of 12.45mm, because the signal will behave according to equation (3) with some modification. In this region the transmitted signal much greater than reflected signal, this phenomenon can be observed in Figure 7-a and Figure 7-b. The matter will be different for region from 12.4587 to 20mm, because the signal will behave according to equation (4) with some modification, wherein the reflected signals will be present and must be taken in calculation. This phenomenon causes fluctuation in E-field for region from 12.45mm to 20mm of muscle tissue.

<table>
<thead>
<tr>
<th>Depth (mm)</th>
<th>4</th>
<th>8</th>
<th>10</th>
<th>12</th>
<th>14</th>
<th>18</th>
</tr>
</thead>
<tbody>
<tr>
<td>Method1 (V/m)</td>
<td>0.5670</td>
<td>0.3342</td>
<td>0.2558</td>
<td>0.2011</td>
<td>0.1435</td>
<td>0.0699</td>
</tr>
<tr>
<td>Method2 (V/m)</td>
<td>0.5675</td>
<td>0.3339</td>
<td>0.2554</td>
<td>0.2005</td>
<td>0.1432</td>
<td>0.0696</td>
</tr>
</tbody>
</table>
5. Discussion and Conclusions

A comparison of the two methods gives same results approximately. The difference between results is ranging from $10^{-3}$ to $10^{-2}$ approximately, this difference can be neglected when using large values of electric field. Therefore, first method is suitable for calculating magnitude of electric field at any point inside muscle or other tissue. Another conclusion is when penetration depth greater than thickness of tissue, the signal will reflect and combine with transmitted signal, therefore, the signal will fluctuate and form standing wave at different points. When penetration depth of muscle smaller than its thickness, the reflected signal from next tissue will be very small, this causes exponential fading for the signal to certain depth, then the penetration depth will be greater than thickness. The signal will fluctuate at this depth, because appearance of reflected signals.

References


