Mechanical Oscillation of the Cam Mechanism

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Abstract This article deals with the dynamic analysis of cam mechanism using MSC Adams. In the first part of this paper is solving the dynamic analysis using the Newtonian mechanics. The mathematical model was designed by using this method of dynamic analysis. The second part deals with the dynamic analysis in the program MSC Adams/View. The dynamic analysis is important in terms usability of cam mechanism.

Keywords: dynamic analysis, cam mechanism, vibration, spring force, spring deformation


1. Introduction

The cam mechanisms have been used for a long time until today and are included as an integral part of combustion engines. They are encountered in installations where comes transformation of rotary movement to movement of shifting in practice. The advantage of cam mechanisms is their simplicity and high functionality. The dynamic analysis of the mechanism with a circular cam is the aim of this work. This analysis is necessary when dealing with design of a cam mechanism it to achieve the best result which means to achieve desired properties when is used the smallest amount of material, for instance.

Mathematical model of the cam mechanism was derived by using Newton’s dynamics. In the second part of the dynamic analysis is solution by program MSC Adams. Programs such as MSC Adams can facilitate dynamic analysis of various complex mechanisms which simplify and velocity up the analysis results. To the desired results solutions leads correctly preparation of dimensional model in a computer program simulation of MSC. That program allows you to evaluate the results in graphical and numerical form. It can determine kinematics quantities such as: displacement, velocity, acceleration, and other physical quantities. The dynamic analysis is important in terms usability of the cam mechanism, because of not every shape and the characteristics of that cam meets the specific mechanism. The graphical course of displacement, velocity and acceleration is suggested to show us the correct function of cam mechanism.

2. Cam Mechanism and Newtonian Mechanics

Our task is to deal with the motion of matter. We need to determine the force transmitted to the resilient member. On the figure is shown the equivalent circuit of cam mechanism with consideration to the follower part with stiffness k. We applied Newton's equations in examining the absolute motion of the mass m in form [1]:

\[ F = m a \]  

(1)

To analyze the vibration, we shall consider the mass m of the cam mechanism shown in the position in Figure 1.

![Figure 1](image-url)

Figure 1. The cam mechanism model

The force exerted by the spring in the position in Figure 1 [2] has a magnitude \( T = k(x - l - y(t)) \). Substituting for \( F \) into the fundamental equation \( F = ma \) and recalling that \( a \) is the second derivative \( x' \) of \( x \) with respect to \( t \), we write:

\[ m \ddot{x} = -k \left( x - l - y(t) \right) \]  

(2)

or we write in the form:

\[ m \ddot{x} + k \left( x - l - y(t) \right) = 0 \]  

(3)

and

\[ m \ddot{x} + \Omega^2 k = f(t) \]  

(4)

where:
the size of angular velocity, circular frequency of the vibration.

Function \( y(t) \) is given by the stroke dependence of the cam \( y(\phi) \) and rotational movement of the cam \( \phi(t) \). In the uniform rotation of the camshaft is \( \omega = \text{const.} \), \( \phi = \omega t \) and the course of movements \( y(t) \) will be periodic functions of time. If we explicate this periodic function with period \( T = \frac{2\pi}{\omega} \) to the Fourier series, we get:

\[
y = y_0 + \sum C_i \sin (i \omega t + \phi_i)
\]  

(5)

Equation of the motion we write in the form:

\[
\ddot{x} + \Omega^2 x = \Omega^2 (l + y_0) + \Omega^2 \sum C_i \sin (i \omega t + \phi_i), \\
i = 1, ..., n
\]

(6)

The stationary part of the oscillation is then given by equation in form:

\[
x = l + y_0 + \sum C_i \sin (i \omega t + \phi_i)
\]

(7)

where:

To calculate the force transmitted by the spring we determine the course of deformation \( \xi(t) \). It is the examination of the relative motion, the equation of motion is:

\[
m \ddot{\xi} = -k \xi - m \dot{y}(t)
\]

(8)

after that

\[
\ddot{\xi} + \Omega^2 \xi = \sum \eta^2 \omega^2 C_i \sin (i \omega t + \phi_i)
\]

(9)

The stationary part of the solution is then given in form:

\[
\xi = \sum \eta^2 \omega^2 C_i \frac{\sin (i \omega t + \phi_i)}{1 - \eta^2}
\]

(10)

The force of the spring is then given by equation in form:

\[
T = k \xi
\]

(11)

This is not only one method of analysis of dynamics which is so difficult; there are also others where solution of movement equation of cam mechanism is not so easy and demanding. Therefore, the use of the program MSC Adams is very advantageous [2].

3. Using MSC Adams/View

With MSC Adams software users can produce virtual prototypes to simulate complex mechanical systems and quickly analyze multiple design variations until an optimal design is achieved. MSC Adams is one of many computer programs for modeling and simulating multi body systems. In programs a virtual prototype of a mechanism show in Figure 2 and Figure 3 can be built and then simulated [3].

If the results, a certain movement or load transmission are not satisfy, the prototype can easily be modified and then simulated again.

Adams is the world’s most widely used multi-body dynamics simulation software. It lets you build and test virtual prototypes, realistically simulating on your computer, both visually and mathematically, the full-motion behavior of your complex mechanical system designs as shown in the Figure 3.
After construction model in MSC Adams/View shown in Figure 2 we could try to simulate the movement of the cam mechanism and to determine the physical properties [4].

The Post Processor processes the results of the solution position, velocity, acceleration of the part_2 (Figure 4), position, velocity of the part_3 (Figure 5), position and velocity of the part_4 (Figure 6).

We have chosen necessary interested variables such as displacement, velocity and acceleration. The next step was to choose the correct folder where variables are investigated. Graphs of the spring deformation and spring force using the MSC Adams program are shown in next figures [5].

The Postprocessor provides complete value at certain time intervals and of course the specific waveforms from which can be read values [6].

The last step of dynamic analysis of cam mechanism was to find out some forces which operate in the spring when is the cam mechanisms in motion. The size and the course of force of spring are shown in Figure 8 and Figure 9 [6,7].
4. Conclusion

In this paper one module of the number of modules namely MSC Adams/View was used as a tool which allows a better simulation and visualization of the model and easier evaluation of the results obtained. With the module MSC Adams/View they represent a tool that is able to addresses various types of mechanisms with many degrees of freedom.

In this article it is shown a procedure for solving kinematics problem of the mechanism using modeling in program MSC Adams View. This program allows simulate moving of such mechanical systems. Results are obtained in form of time diagram of the desired variables. Tasks are solved numerically. Model is compiled by using program MSC Adams View [6]. The results are obtained by the simulation of cam mechanism were processed by the postprocessor program of MSC Adams/View. Program

MSC Adams/View makes it easy to analyze complex mechanical systems with multiple degrees of freedom.

Mastering this methodology provides a suitable tool for solving problems of teaching and practice. The contribution of this work is mainly didactic. Especially in the field of Applied Mechanics, presents the possibility of computer simulation.

Acknowledgement

This work was supported by the Ministry of Education of the Slovakia Foundation under Grant VEGA No. 1/1205/12 and VEGA No. 1/0937/12.

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