Optical Analysis in CH$_3$NH$_3$PbI$_3$ and CH$_3$NH$_3$PbI$_2$Cl Based Thin-Film Perovskite Solar Cell

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Abstract The optics of organic-inorganic halide perovskites materials in thin-film smooth surface p-i-n solar cell has been studied. The study was conducted for CH$_3$NH$_3$PbI$_3$ perovskite material, used as a photoactive layer and sandwiched between ultrathin electron transport layer of TiO$_2$ and hole transport layer of P3HT. The investigation was carried out based on the optical wave propagation simulation results of quantum efficiency and short circuit current. A reference model of solar cell exhibits a maximum of 21.79 mA/cm$^2$ short circuit current as well as 76% of external quantum efficiency (EQE) for 620 nm to 700 nm of spectral range of wavelengths. Analyzing the influence of thickness for each layer on the short circuit current and the quantum efficiency the cell was optimized. Finally, a comparative analysis has also been done between CH$_3$NH$_3$PbI$_3$ and CH$_3$NH$_3$PbI$_2$Cl perovskite thin-film solar cell, where CH$_3$NH$_3$PbI$_2$Cl based solar cell gives 2.7% higher short circuit current and around 7.5% higher photon absorption, particularly in the near infrared red regions of spectrum (700 nm - 800 nm) and for the 360 nm of absorbing layer. Throughout the research, a Finite Difference Time Domain (FDTD) based Maxwell’s curl equations solver was used.

Keywords: perovskite solar cell, CH$_3$NH$_3$PbI$_3$-Cl$_x$, quantum efficiency, short circuit current, FDTD


1. Introduction

Photovoltaic effect is one of the most effective methods of converting solar energy into electrical energy using solar cells. Although the conventional crystalline silicon or GaAs based single junction solar cells have already been reached to 27.6% of conversion efficiency and multi-junction crystalline solar cell is even more [1], a comparatively very high synthesis and manufacturing costs of photovoltaic cells is limiting the large scale use in real. The necessity of finding high efficiency alternating and cheap sources of energy has made the organometallic halide perovskites (e.g., CH$_3$NH$_3$PbI$_3$ and CH$_3$NH$_3$PbI$_2$Cl) based thin-film solar cell as one of the most promising candidate. A very high band-gap, large range of absorption coefficient, light harvesting capability and power conversion efficiency of this new type of solar cells has already surpassed organic and dye-sensitized solar cells. The theoretical efficiency has just incredibly increased from 3.8% to more than 17% in only last couple of 2 years in single and double junction perovskite solar cells [2,3,4,5]. Unlike the organic and dye-sensitized solar cell the perovskite solar cell is non-excitonic due to the lower exciton-binding energy (<50 meV), having ultrafast interfacial charge-transfer speed and electron- and hole-diffusion lengths between 100 nm and a micron [6,7,8].

So, better electrical and optical performances can be achieved for a few more hundreds of nanometers of perovskite geometry.

In this manuscript, the optics in thin-film CH$_3$NH$_3$PbI$_3$ perovskite solar cell has been investigated and optimized for the best possible output by analyzing the influence of thickness on upper limit external quantum efficiency and short circuit current. Then a comparative analysis on losses in every layer has also been carried out between CH$_3$NH$_3$PbI$_3$ and CH$_3$NH$_3$PbI$_2$Cl absorbing layer of perovskite thin-film solar cells.

2. Optical Structure Modeling

The optical wave propagation simulations have been performed for thin-film perovskite solar cells on smooth substrate. A schematic cross section of perovskite solar cell on smooth substrate is depicted in Figure 1(a). The perovskite photovoltaic cell structure, investigated in this study, consists of a 130 nm indium tin oxide (ITO) front contact, followed by a 50 nm electron transport layer, TiO$_2$, a 360 nm photoactive perovskite material of CH$_3$NH$_3$PbI$_3$, a 50 nm hole transport layer of P$_3$HT (poly (3-n-hexylthiophene)), and a 100 nm Au metal back contact. Simulations were carried out for two dimensional (2D) case, where the simulation environment was created based on finite difference time domain (FDTD) method.
The Maxwell’s equations were rigorously solved for the electric field calculation. Since a two dimensional FDTD algorithm was utilized, it splits the Maxwell’s equations into two independent sets of equations for transverse electric (TE) and transverse magnetic (TM) polarized waves. The polarization of the input wave was assumed to be TE, thus only one component of the electric field, $E_Z$, had to be solved. In order to achieve better absorption, perfect matched layer (PML) boundary was assumed in $z$-direction during simulation time. The simulation environment calculates the electrical field inside the proposed structures. In order to obtain the characteristic efficiency parameters in which we were interested, some further processing of this raw data must be performed. In this section, results are shown depending on device structure.

![Figure 1](image-url)

**Figure 1.** (a) Schematic cross section of simulated perovskite solar cell on smooth substrate; corresponding power loss profile for monochromatic illumination of wavelength (b) 400 nm, and (c) 700 nm

The time average power loss map within p-i-n superstrate configuration solar cell is shown in Figure 1(b) and 1(c). The incident wavelengths were 400 nm and 700 nm. It was calculated for an incident wave with an amplitude of 1 V/m. For the shorter wavelengths, CH$_3$NH$_3$PbI$_3$ has higher extinction or absorption coefficient. As a consequence, most of the lights are absorbed at the interface of TiO$_2$ and CH$_3$NH$_3$PbI$_3$ layer and then some of the light is absorbed in the bulk of the active layer. However, very few power loss was observed at ITO, TiO$_2$, and P3HT due to the presence of a small optical behavior in shorter wavelengths. Whereas, the absorption in the absorbing perovskite layer in 700 nm is comparatively higher than 400 nm since the extinction coefficient for the CH$_3$NH$_3$PbI$_3$ material is very high and it absorbs the maximum incoming light for the red or infrared red part of wavelength spectrum. Although ITO and TiO$_2$ are almost transparent for longer wavelengths of optical spectrum, there is a small amount of parasitic absorption loss in P3HT and its total loss can be calculated as almost 8.15%.

In organic-inorganic halide perovskite solar cells, the internal quantum efficiency is assumed to be 100%. Therefore, the determined quantum efficiency defines an upper limit of the achievable external quantum efficiency. The quantum efficiency for a perovskite solar cell can be calculated as the ratio of the power absorbed in the perovskite absorber material to the total power incident ($P_{Opt}$) on the unit cell. The following equation (2) was used to calculate the quantum efficiency:

$$QE = \frac{1}{P_{Opt}} \int Q(x,y) \, dx \, dy$$

where $Q(x,z) = \frac{1}{2} c_0 \alpha |E(x,z)|^2$.
The short circuit current was calculated based on the external quantum efficiency using the following equation (3):

$$I_{SC} = \frac{q}{hc} \int_{\lambda_{min}}^{\lambda_{max}} \lambda \cdot QE(\lambda) \cdot S(\lambda) d\lambda$$

where $h$ is Planck’s constant, $c$ is the light velocity, $q$ is the elementary charge, $\lambda$ is the wavelength, and $S(\lambda)$ is the spectral irradiance of sunlight (AM 1.5).

3. Optimization of Perovskite Solar Cell

In order to optimize i.e., to maximize the short circuit current and quantum efficiency of the perovskite solar cell on smooth substrate, the influence of the variation of thickness of TiO$_2$, CH$_3$NH$_3$PbI$_3$, and P$_3$HT layers on quantum efficiency and short circuit current was studied using the FDTD method.

![Figure 2](image2.png)

**Figure 2.** Short circuit current as a function of the thickness of TiO$_2$. Corresponding comparison of quantum efficiency for perovskite based solar cell with the variation of TiO$_2$ layer thickness (Inset)

TiO$_2$ layer thickness was varied in between 0 nm and 100 nm, while perovskite layer and other layer thicknesses were kept constant. The simulated short circuit current as a function of the TiO$_2$ layer thickness along with the external quantum efficiency as a function of wavelength range 300 - 800 nm (inset) are depicted in Figure 2. The variation of the TiO$_2$ layer thickness has a great influence on the short circuit current. The short circuit current increases with the increase of thickness up to 40 nm and it decreases and becomes almost saturated after 40 nm. This is due to the fact that the photon absorption in perovskite photoactive material for the red and infrared red part of light spectrum is very poor and most of the light is absorbed in the blue region (300 nm - 400 nm) below the 40 nm of the TiO$_2$ thickness. As the thickness increases the absorption increases mainly in the 600 nm - 800 nm of the wavelength spectrum. So, above the 40 nm thickness of the TiO$_2$ layer has hardly any influence on the device performance since its absorption in the visible range and the change of short circuit current are negligible and the reflection coefficient at the ITO/TiO$_2$ interface is low so that interference effects that depend on the TiO$_2$ thickness play a minor role. However, a maximum short circuit current density of 21.42 mA/cm$^2$ can be achieved at 40 nm of TiO$_2$, having maximum about 92.4% of external quantum efficiency at 520 nm.

P$_3$HT is particularly used as a hole transport layer, which is also varied in 0 nm to 100 nm for the investigation. By varying the thickness of P$_3$HT layer, we actually vary the distance of the active region to the reflecting Au metal electrode since P$_3$HT has also absorption and carriers generation capability, thereby driving the active region through a pronounced interference pattern [9]. The calculated short circuit current density and external quantum efficiency (inset) are inscribed in Figure 3. At 10 nm thickness of ultrathin P$_3$HT layer, the short circuit current density and quantum efficiency are maximum i.e., the photoactive region is placed at the maximum of the optical field distribution and the short circuit current has a maximum value of 21.9 mA/cm$^2$. With increasing P$_3$HT thickness the short circuit current decreases, having a minimum value of about 20.5 mA/cm$^2$ at 100 nm of thickness. However, the photon absorption in the absorbing material decreases with the increase of the layer thickness, especially in the longer wavelengths (600 - 750 nm).

![Figure 3](image3.png)

**Figure 3.** Short circuit current as a function of the thickness of P$_3$HT. Corresponding comparison of quantum efficiency for perovskite based solar cell with the variation of P$_3$HT layer thickness (Inset)

The influence of the perovskite absorber layer thickness on the short circuit current and the quantum efficiency (inset) is shown in Figure 4. The thickness of the CH$_3$NH$_3$PbI$_3$ layer was varied from 100 nm to 600 nm, whereas thickness for other layers were kept constant. As the thickness of the perovskite layer is increased, a significant increase of the short circuit current as well as the quantum efficiency was observed. For a solar cell active layer thickness of 600 nm, the short circuit current increases from around 15.5 mA/cm$^2$ to 22.7 mA/cm$^2$. A significant amount of light absorption is also observed almost in the whole wavelength spectrum (450 nm - 750 nm) depicted in Figure 4 (inset). But we cannot merely increase the thickness of the absorber material due to the shorting defects that arises from the large crystals and it might create additional defects in the band gap acting as recombination centers for photogenerated carriers, which in turn deteriorates its electrical properties [8]. Hence 360
nm perovskite layer has been predicted as the optimum thickness for the further investigation.

The optimized process of perovskite planar solar cell structure has been carried out by mainly observing the influence of thickness for different layers of the cell. Based on the best short circuit current and quantum efficiency, an optimal solar cell layer sequence, ITO(130 nm)/TiO2 (40 nm)/CH3NH3PbI3 (360 nm)/P3HT (10 nm)/Au (100 nm), has been obtained. The optimal flat solar cell structure leads to an increase of the short circuit current by 0.26 mA/cm2, resulting in a short circuit current density of 22.05 mA/cm2. The quantum efficiency plot for the optimized perovskite solar cell with smooth surface along with parasitic absorption losses in different layers is depicted in Figure 5. The optimal structure exhibits an advantage of the quantum efficiency in the region of 550 nm - 700 nm, since the structure was adjusted by obtaining mainly the best thickness of P3HT layer which has better absorption in that region.

The optimized cell has a very low absorption in the TiO2, P3HT, and Au compared to ITO. The maximum quantum efficiency about 93% can be obtained in 490 nm-540 nm of wavelength spectrum. In terms of the parasitic absorptions, the ITO, TiO2, P3HT, and Au metal layers absorb 0.62%, 0.028%, 0.067%, and 0.11%, respectively at 510 nm, whereas CH3NH3PbI3 absorbs almost 93.7% of the total absorbed light in the entire solar cell stack. The largest loss is observed for ITO layer mainly for the shorter wavelengths (300 – 400 nm), while it is almost transparent in 400 nm - 700 nm of optical spectral range. However, the total optical loss increases for the longer wavelengths though it is very low for the shorter wavelengths. The reflection can be calculated as R = 1 − A, where A is the total absorption of the solar cell. It can be observed that the upper portion of the quantum efficiency curve is white, representing the total reflection from the solar cell.

4. Comparative Analysis of CH3NH3PbI2Cl and CH3NH3PbI3 Perovskite Solar Cells

In this section, the comparison of CH3NH3PbI3 and CH3NH3PbI2Cl based perovskite thin-film solar cell was studied. The comparison was carried out based on the simulated quantum efficiency, short circuit current density, and parasitic absorption losses in each layer. A comparative short circuit current and quantum efficiency plots are depicted in Figure 6(a) and Figure 6(b). By using CH3NH3PbI2Cl perovskite photoactive material, an enhancement of quantum efficiency is pronounced in the longer wavelengths (700 nm-800 nm) due to the better incoupling of light to the absorber layer. Moreover, the diffusion length of the CH3NH3PbI2Cl perovskite absorber is much more higher than CH3NH3PbI3 perovskite material, which enhances the volume of the space charge region and increases size of the effective thickness, therefore allowing more carriers to be dissociated into free charges. However, for the shorter wavelengths (300 nm-700 nm) there is no significant difference of light absorption in the active layer between CH3NH3PbI2Cl and CH3NH3PbI3 perovskite solar cell. Compared to the short circuit current values obtained for CH3NH3PbI3 solar cell over the variation of the absorber layer thickness, the current values calculated from CH3NH3PbI2Cl perovskite solar cell is higher by around 2.5% almost all the way in the range from 360 nm to the 700 nm thickness of the absorbing layer.

The short circuit current gain can be calculated as about 0.40 mA/cm2. This is due to the fact that the carrier lifetime along with multiple passes or bounces of incident light ray increases by using CH3NH3PbI2Cl, consequently the absorption in the absorber layer increases as well. Moreover, the parasitic absorption losses are drastically decreased in the hole transport layer (P3HT) and back contact (Au) layer of the solar cell as inscribed in Figure 7(c) & (d). The parasitic absorption loss in the P3HT layer for the CH3NH3PbI3 perovskite solar cell was calculated as 9.04%, whereas it is only 5.7% for CH3NH3PbI2Cl perovskite solar cell in the 600 nm of wavelength. On an average about 2.18% of higher parasitic absorption loss is
pronounced in the Au layer for the CH$_3$NH$_3$PbI$_3$ perovskite solar cell, compared with CH$_3$NH$_3$PbI$_2$Cl perovskite solar cell mainly in the longer wavelengths (600 nm - 800 nm). However, losses are almost same in the ITO and TiO$_2$ layer shown in Figure 7 (a) & (b).

![Figure 6](image_url)

**Figure 6.** a) Comparison of short circuit current with the variation of perovskite based thin film solar cell with and without Cl; b) Comparison of quantum efficiency plots for 360 nm of perovskite based thin film solar cell with and without Cl

![Figure 7](image_url)

**Figure 7.** Comparison of parasitic absorption losses between CH$_3$NH$_3$PbI$_2$Cl and CH$_3$NH$_3$PbI perovskite based thin-film solar cells in a) ITO, b) TiO$_2$, c) P$_3$HT, and d) Au layers

5. Conclusion

The study of thin-film perovskite photovoltaic cell was started with the optimization of simple planar surface solar cell by analyzing the influence of the variation of the thickness in different layers on short circuit current and quantum efficiency using finite difference time domain (FDTD) method. The optimized cell achieves maximum of 22.05 mA/cm$^2$ short circuit current density with 93% of external quantum efficiency in the 530 nm of wavelength spectrum. P$_3$HT plays a major role in optimizing the cell since it exhibits an advantage of the quantum efficiency in
the region of 550 nm - 700 nm. It has also come to realize that the overall gain of the CH$_3$NH$_3$PbI$_2$Cl based perovskite solar cell is higher than CH$_3$NH$_3$PbI$_3$ perovskite solar cell due to the higher carrier diffusion length, optical effective thickness, and absorption capability mainly in the longer wavelength range (700 nm-800 nm). However, the knowledge of optics studied in this research on this excellent perovskite thin-film solar cell can be implemented in high efficiency tandem devices. Since perovskite material could be used as an excellent top cell along with suitable Si material as bottom cell, which would link into existing, extensive research activities all over the world into high efficiency, back contact Si solar cells.

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