Estimation of the Yield Stress of Cement Pastes from Electrical Resistivity Measurement

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Abstract This study proposes a continuous method for predicting the yield stress development from mixing until the final setting point. Samples prepared with water to cement ratios (w/c) of 0.3, 0.35 and 0.4 are tested using a vane in cup rheometer, a Vicat needle and a non contact electrical resistivity machine (NC-ERM). Times corresponding to the initial yield stress (ta), a dramatic increase in the yield stress (tb), a maximum torque reading on the rheometer (tc), an initial setting (td) and a final setting (te) on the yield stress-time (τ(t)-t) curve are correlated with the time at a point of inflexion (tp) on the bulk resistivity-time (ρ(t)-t) curve. A quantitative relationship developed between the yield stress and electrical resistivity shows a good agreement with experimental data.

Keywords: electrical resistivity, yield stress, cement paste, water to binder ratio


1. Introduction and Methodology

1.1. Introduction

There is a need for the continuous quality control of workmanship and materials at a modern construction site. The performance of concrete during pumping, spreading, molding and compaction can be inferred from the yield stress of a cement paste behavior before hardening [1]. The yield stress of cement pastes in a very fluid state has been evaluated by mini slump cone [2,3,4,5], marsh cone [6,7,8,9] and rheometers [10,11,12]. Recent researches have shown that there is a relationship between setting time as determined empirically by a Vicat needle and shear yield stress [13,14,15], Liao et al [16] has gone ahead to determine the yield stress at initial setting time and final setting time as 32.4kPa and 780kPa respectively [16].

The mini slump cone, Vicat needle and marsh cone are relatively affordable, reliable and require less skilled labor to operate in comparison with a rheometer. However, all methods discussed require several discrete measurements on the sample to gain an understanding of the development of yield stress with the time. Furthermore, rheometers of different configuration report different values of the yield stress even for the same sample, although the trend of change may be similar [17]. The limited range of the rheometers and insensitivity of the Vicat apparatus at a low yield stress (<18kPa) has been highlighted by the reference [18].

The objective of this study is to propose an alternative method based on the electrical resistivity to evaluate a yield stress of cement pastes over a wider range of fluidity than the methods discussed earlier. We utilized a Non Contacting Electrical Resistivity Machine (NC-ERM) that was invented by Li and Li [19] and manufactured by Hong Kong Brilliant Concept Technologies. Liu et al [20] and Wei et al [21,22] have previously used the apparatus successfully that used to study the hydration of cementitious materials [20,21,22]. It overcomes major drawbacks of an alternative electrical resistivity apparatus such as polarization due to DC currents and a poor contact between the sample and probes. The machine consists of a transformer that generates a voltage across the primary coil. This induces a voltage across the sample (secondary coil). The current across the sample is measured by a current meter and resistivity of cement sample computed from Ohms law.

1.2. Methodology

The typical yield stress and an electrical resistivity development with time curves are shown in Figure 1(a) and Figure 1(b), respectively. From Figure 1(a), the general development of the yield stress with time is a four stage process separated by characteristic points B, C and D. The yield stress in the stages AB, BC, and CD has been shown to be linear [18]. For the case of this study, a linear growth of the shear yield stress is assumed between the torque limit of the rheometer and the initial setting, D due to lack of a suitable apparatus to measure its evolution. In the stage DE, a yield stress from Vicat needle penetration has been shown to fit a parabolic curve [16]. The evolution of a yield stress of cement pastes is largely affected by a porosity reduction which is reflected by a three dimensional network that often forms due to flocculation [23]. Similarly, the reduction in porosity results in an increase in resistivity between points M and P as shown in Figure 1(b). This period has been understood to include the dormant and acceleration stages of hydration [24,25,26].
It is upon this background that a relationship between the yield stress and the electrical resistivity is formulated as illustrated in Figure 2 and computed according to the following steps:

Step 1: The critical times from the yield stress curve are expressed as a function (g) of time, $t_p$, from the resistivity curve by a linear regression as expressed in Eq. (1).

Step 2: From the equation of $\tau (t)$ obtained from $\tau (t) - t$ and the relationship between yield stress critical times and $t_p$ from the resistivity curve, yield stress is expressed in terms of $t_p$.

Step 3: The influence of water to cement ratio (w/c) is incorporated and the general equation is given by Eq. (2).

Figure 1. Typical development with time of (a) yield stress (b) electrical resistivity and rate of resistivity

Figure 2. Algorithm to predict yield stress from electrical resistivity
2. Materials and Samples Preparation

2.1. Materials

P·O 42.5 that meets the requirements of Chinese cement standard GB/T17671-1999 was used for this study. Its chemical properties are shown in Table 1. Distilled water was used throughout the experiment.

<table>
<thead>
<tr>
<th>Oxide</th>
<th>CaO</th>
<th>SiO₂</th>
<th>Al₂O₃</th>
<th>Fe₂O₃</th>
<th>MgO</th>
<th>SO₃</th>
<th>Na₂O</th>
<th>K₂O</th>
<th>LOI</th>
</tr>
</thead>
<tbody>
<tr>
<td>Weight(%)</td>
<td>63.02</td>
<td>21.88</td>
<td>4.02</td>
<td>2.59</td>
<td>2.44</td>
<td>3.10</td>
<td>0.32</td>
<td>0.15</td>
<td>1.68</td>
</tr>
</tbody>
</table>

2.2. Samples Preparation

Pastes for all the three experiments were mixed using a planetary mixer in the laboratory. The mixing program consisted of a slow mixing at 45 rpm for 120 seconds followed by a fast mixing at 90 rpm for a further another 120 seconds. There was a 15 seconds interval between the two mixing regimes to allow for cleaning. The samples are mixed with water to cement ratios (w/c) of 0.3, 0.35 and 0.4 and labeled as W 0.3, W 0.35 and W 0.4, respectively.

3. Experimental

3.1. Rheology

A vane in cup rheometer (Brookfield SST 2000) was used to monitor the stress growth with time. After mixing in the planetary mixer, samples were prepared in glass cylinders and pre-sheared at 150 Pa for 60 seconds to establish the uniform microstructure. The vane used had a diameter of 15 mm and height of 30 mm and the gap between the vane and the walls of the cylinder was 10 mm. The temperature in the room was maintained at 200°C using an air conditioner and all samples were covered with a moist cloth to prevent evaporation. To determine the yield stress after a period of time, a constant shear rate of 0.01S⁻¹ was applied [27] and the yield stress is determined as the maximum shear stress on the shear stress-time plot [28].

3.2. Vicat Needle

The test was performed according to ASTM C191. In this paper, however, the cement paste was not of standard consistency but of water to cement ratios 0.3, 0.35 and 0.4 as required for all the other tests on the yield stress and the electrical resistivity [29].

3.3. Electrical Resistivity

The apparatus used is illustrated in Figure 3. Each sample is placed in a plastic mold and tested up to 24 hours using a procedure adopted by Xiao et al [26]. Each sample is prepared in the same way as the one used for the rheological measurement and the Vicat penetration. Data points are collected continuously every minute and recorded by a computer. The method is versatile for its ability to continuously monitor the cement paste hydration without having to destroy the bonds that are formed.

![Figure 3. Schematic of Non Contacting Electrical Resistivity Machine (NC-ERM)](image)

<table>
<thead>
<tr>
<th>Sample</th>
<th>Rheology</th>
<th>Vicat Needle</th>
<th>Resistivity</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>tₐ</td>
<td>t₉</td>
<td>t₉</td>
</tr>
<tr>
<td>W0.3</td>
<td>10</td>
<td>86</td>
<td>150</td>
</tr>
<tr>
<td>W0.35</td>
<td>10</td>
<td>118</td>
<td>180</td>
</tr>
<tr>
<td>W0.4</td>
<td>10</td>
<td>149</td>
<td>210</td>
</tr>
</tbody>
</table>

4. Results and Discussions

4.1. Rheological Measurements

A summary of all the critical points from the rheometer, Vicat needle and the resistivity measurements is presented in Table 2.
rises steadily to a maximum value of 1131 Pa before dropping rapidly. This agrees with what is expected from the operation manual for slurries such as cement paste [28], where the shear stress rises to yield stress and drops thereafter due to the microstructure breaks down. The yield stresses obtained at intervals of 30 minutes are plotted against the hydration time in Figure 5. It is interesting to note that the abrupt change in a slope at point B occurs at approximately the same yield stress for all the samples (~900Pa). In the stage AB, the rate of gain of the shear resistance is of 1 order of magnitude but quickly changes to an order of 10 in the stage BC for all the samples as listed in Table 3. The change in the rate of gain of shear resistance at the point B has been interpreted to be the onset of setting [18,30].

![Figure 4. Typical shear stress with time (w/c=0.3, t=90 min)](image)

**Table 3. Analysis of yield stress curve for all samples**

<table>
<thead>
<tr>
<th>Sample</th>
<th>Rate of gain of stress (Pa/min)</th>
<th>n</th>
<th>L</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>AB</td>
<td>BC</td>
<td>CD</td>
</tr>
<tr>
<td>W0.3</td>
<td>8.1</td>
<td>53.9</td>
<td>596.8</td>
</tr>
<tr>
<td>W0.35</td>
<td>7.25</td>
<td>56.0</td>
<td>289.1</td>
</tr>
<tr>
<td>W0.4</td>
<td>5.741</td>
<td>57.37</td>
<td>329</td>
</tr>
</tbody>
</table>

![Figure 5. Yield stress against time from a rheometer](image)

The water to cement ratio has a pronounced effect on the occurrence of characteristic points B and C as depicted in Figure 5. Samples prepared with a w/c of 0.4 (W 0.4) hydrated for the longest time before the drastic change in the rate of stress development. The point B for the sample W 0.4 occurred at 149 min, and 31 minutes is longer than W 0.35 and 63 minutes and later than the W 0.3. This is an indication of delay in strength development with water fraction which is consistent with cement chemistry. Roussel et al [31] discussed the forces that could be responsible for the development of the yield stress in cement paste namely; colloidal interactions, Brownian forces, and hydrodynamic forces and other contact forces. However, of these, the gain of permanent shear resistance was demonstrated to be a consequence of hydration [32]. Thus, the delay in occurrence of points B and C in Figure 5 indicates a lower degree of hydration in samples with a higher water to cement ratio.
4.2. Vicat Results

Figure 6 shows the typical depth of penetration of the Vicat needle with time for sample W 0.3. It can clearly be seen that the penetration is 40 mm from initial time of mixing until 135 minutes when it begins to decreasing with time. Figure 7 illustrates the development of yield stress which is computed from the penetration depth using Eq. (3) that was adopted by Liao et al. [16]. This points out that the depth of penetration reduces with the increase in the shear resistance.

Where: \( m \) is the mass of the needle (300 grams), \( g \) is the acceleration due to gravity, \( r \) is the radius of the needle (0.565 mm) and \( h \) is the depth of penetration.

Furthermore, the yield stress at the sensitivity threshold of the Vicat needle is 20 kPa from Eq. (3). Consequently not until the cement paste can develop the shear resistance of 20 kPa, will the Vicat needle measure resistance to penetration. This explains the complete penetration of the needle for over two hours after mixing in Figure 6. The curves of best fit in the stage DE for the development of the yield stress with time in Figure 7 can be approximated to a parabolic curve with a variable \( L \). It is dependent on water to cement ratio as shown in Eq. (4) and listed in Table 3.

The initial setting (\( t_d \)) and final setting times (\( t_e \)) are sensitive to the water cement ratio as expected. Points \( D \) and \( E \) are seen in Figure 7 to shift right with an increase in \( w/c \) ratio. This is probably due to the increased pore space for the larger water particle in comparison with the cement particle. The larger inter-particle spaces need to be filled by hydration products before the paste is dense enough to support load.

More pertinent to this study, the initial setting time as indicated by the sharp change in gradient at the point \( B \), \( t_b \) (Figure 5) occurs more than 60 minutes earlier than initial setting time as detected by the Vicat needle (Figure 7). This is consistent with work by reference [30], who put forward the greater sensitivity of the rheometer as the reason for divergence in values reported by the two apparatus.

4.3. Resistivity

The bulk electrical resistivity development curve with time (is shown in Figure 8 and its differential curve (which represents the rate of resistivity development is shown in Figure 9. The minimum point, \( M \) and the inflection point \( P \) are marked on Figure 8 and Figure 9.
respectively. The characteristic time, \( t_p \) at which the peak occurred for all the samples is listed in Table 2. More detail on how to determine critical points is shown in a research by Xiao et al [33]. From the Figure 9, it is observed that from M onwards, the resistivity increases with time for all samples considered. All the electrical development curves are S shaped, having an initial resistivity of about 1 ohm. m which reduces to a minimum value in the same order at the point M. However, from the point M towards the point P, the resistivity increases rapidly as demonstrated by the rate of the resistivity curve in Figure 9. Beyond P, the resistivity continues to increase indefinitely but at a reducing rate and the curves can be approximated to a parabolic curve. The difference in resistivity is more pronounced as the time increases. For instance, there is barely a noticeable difference in resistivity at the point M. However, at the point P the difference is all too pronounced.

By considering the development of the resistivity as a time series, the time \( t_p \) is seen to have a close relationship with the water to cement ratio; \( t_p \) considerably lags with an increase of the w/c. Li et al [34] used similar apparatus [34] and showed a compelling evidence to suggest that the lag in the electrical resistivity and rate of resistivity development lends itself to the porosity reduction that is revealed by the reduced gel/space ratio, they went on to show that the time between points M and P as pointed out on Figure 9 consists of the dormant and acceleration phase of the hydration process.

4.4. Relationship between Electrical Resistivity and Yield Stress

Figure 5 and Figure 7 exhibit a delay in the yield stress with an increase in w/c. Similarly, Figure 8 reveals a lag in the point P on the resistivity-time curve. By looking at the influence of w/c on the yield stress and electrical resistivity, the relationship between the critical time \( tp \) and the yield stress characteristic times \( K \) is proposed in Figure 10. It is evident that there exists a linear relationship between \( K \) and \( tp \) at all measurements taken and as such it can be deduced that both \( K \) and \( tp \) are clearly affected by the w/c. This relationship lays a framework upon which the yield stress is characterized from the electrical resistivity based on the assumption that the major factor affecting both is the porosity development.

By breaking down the development of yield stress into the time domain and w/c ratio domains, the yield stress is given out as a function of time and w/c ratio as shown in Eq. (5). Generally speaking, the yield stress and electrical resistivity reduce with w/c and increase with time.
Furthermore, the contribution of porosity to the yield stress can be explained by packing density. For instance, the yield stress of W0.3 at 10 minutes after mixing (284Pa) is 2.95 times that of W0.35 and 5.46 times that of W0.4. The solid volume fractions of cement paste, where \( \rho \) and \( \rho_{w} \) are the densities of cement and water, respectively. They are computed as 0.52, 0.48, and 0.45 for samples W0.3, W0.35 and W0.4, respectively. This indicates a higher porosity for sample W0.4 compared to W0.3 thus a lower yield stress. Sak et al [35] and Bui et al [36] suggested that the proximity of the particles is responsible for stronger Van der waals forces in samples with lower water cement ratio [35,36]. This assertion is supported by the calculated solid volume fraction of cement.

4.5. The Validation of a Mathematical Model

A robust non contact electrical resistivity method has been employed to monitor the cement paste hydration and correlate with a yield stress measured by a Vicat needle and a vane in cup rheometer (Brookfield SST 2000). The effects of water to cement ratio and time are examined and modeled in Eq. (5).

The model suggested in Eq. (5) is validated with data for a sample of w/c=0.3 during the stage AB at t=10, 30 and 60 minutes. It is seen that the predicted values are within 5 % of the measured values as shown in Figure 11. The yield stress can be reliably predicted from an electrical resistivity using the time corresponding to the peak point P.

5. Conclusions

Within the experimental range, the findings of this study are as follows:

1. The increase in w/c ratio delays both the yield stress and the electrical resistivity development with time. This can be attributed to the increased porosity that affects both yield stress and electrical resistivity of cement pastes.

2. The linear relationship between the yield stress critical times, \( K \) and the characteristic time, \( t_{p} \) on the resistivity curve is a further indication that both yield stress and electrical resistivity reduce with w/c and increase with time.

3. The empirical relationship between the electrical resistivity development and the yield stress growth has been put forward and it shows a good agreement with experimental data.

4. The method suggested in this study has the potential to evaluate the yield stress from mixing until the final setting time. This makes it more applicable over a wide range of fluidity than the mini slump cone, marsh cone, Vicat needle and most available rheometers.
Acknowledgement

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References


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